



Temperature Property Analysis of Micro Flow Sensor using  
Thermal Transfer Equation

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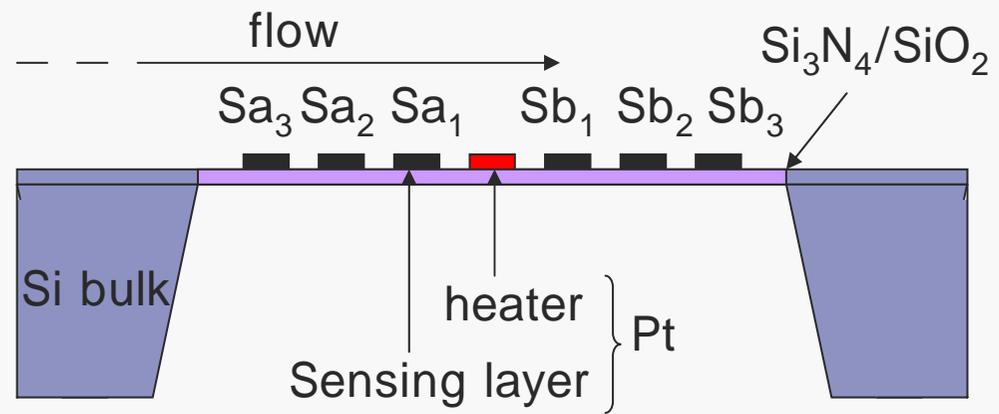
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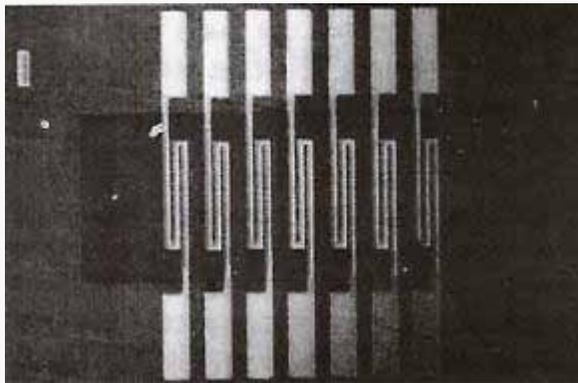
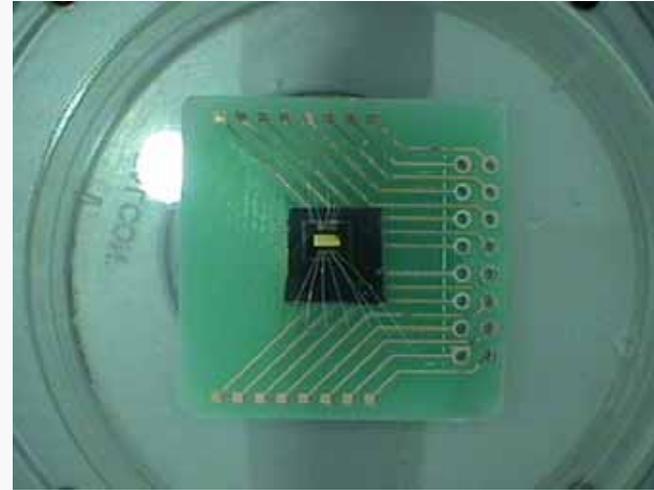
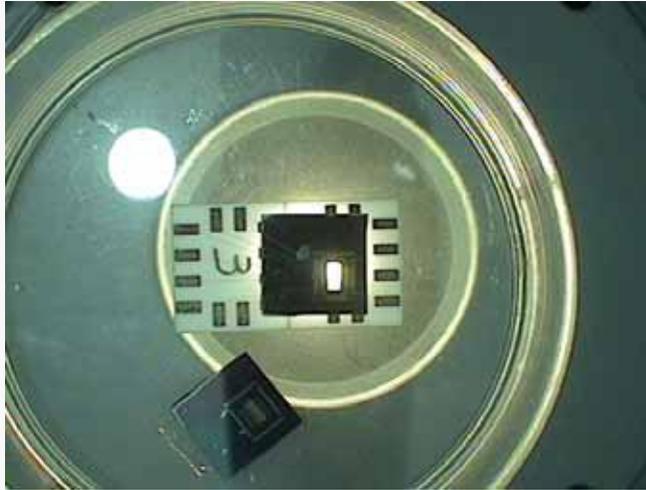
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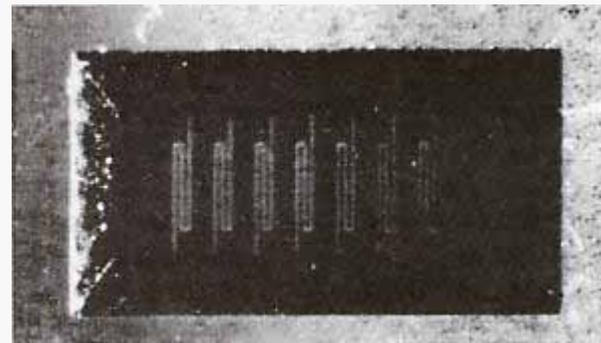
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Top view

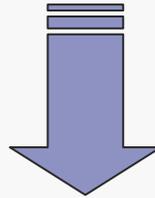


Bottom side

# Thermal Transfer Equation

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$$\frac{\partial T}{\partial t} + \frac{\partial(uT)}{\partial x} + \frac{\partial(vT)}{\partial y} - \alpha_x \frac{\partial^2 T}{\partial x^2} - \alpha_y \frac{\partial^2 T}{\partial y^2} = 0$$



$$\frac{\partial T}{\partial t} + u \frac{\partial T}{\partial x} + v \frac{\partial T}{\partial y} - \alpha_x \frac{\partial^2 T}{\partial x^2} - \alpha_y \frac{\partial^2 T}{\partial y^2} = 0$$

Convection terms

Diffusion terms

# Thermal Transfer Equation

$$\frac{\partial T}{\partial t} = \frac{T_{j,k}^{p+1} - T_{j,k}^p}{\Delta t}$$

$$\alpha_x \frac{\partial^2 T}{\partial x^2} = \alpha_x \frac{T_{j-1,k}^p - 2T_{j,k}^p + T_{j+1,k}^p}{\Delta x^2}$$

$$u \frac{\partial T}{\partial x} = u \frac{T_{j+1,k}^p - T_{j-1,k}^p}{2\Delta x}$$

$$\alpha_y \frac{\partial^2 T}{\partial y^2} = \alpha_y \frac{T_{j,k-1}^p - 2T_{j,k}^p + T_{j,k+1}^p}{\Delta y^2}$$

$$v \frac{\partial T}{\partial y} = v \frac{T_{j,k+1}^p - T_{j,k-1}^p}{2\Delta y}$$

$$S_x = \frac{\alpha_x \Delta t}{\Delta x^2}, \quad S_y = \frac{\alpha_y \Delta t}{\Delta y^2}$$

$$C_x = \frac{u \Delta t}{\Delta x}, \quad C_y = \frac{v \Delta t}{\Delta y}$$

$$\begin{aligned} T_{j,k}^{p+1} = & (S_x + 0.5C_x)T_{j-1,k}^p + (S_x - 0.5C_x)T_{j+1,k}^p \\ & + (1 - 2S_x - 2S_y)T_{j,k}^p \\ & + (S_y + 0.5C_x)T_{j,k-1}^p + (S_y - 0.5C_x)T_{j,k+1}^p \end{aligned}$$

Von Neumann

$$: (S_x + S_y) \leq 0.5, \quad \frac{C_x^2}{S_x} + \frac{C_y^2}{S_y} \leq 2$$



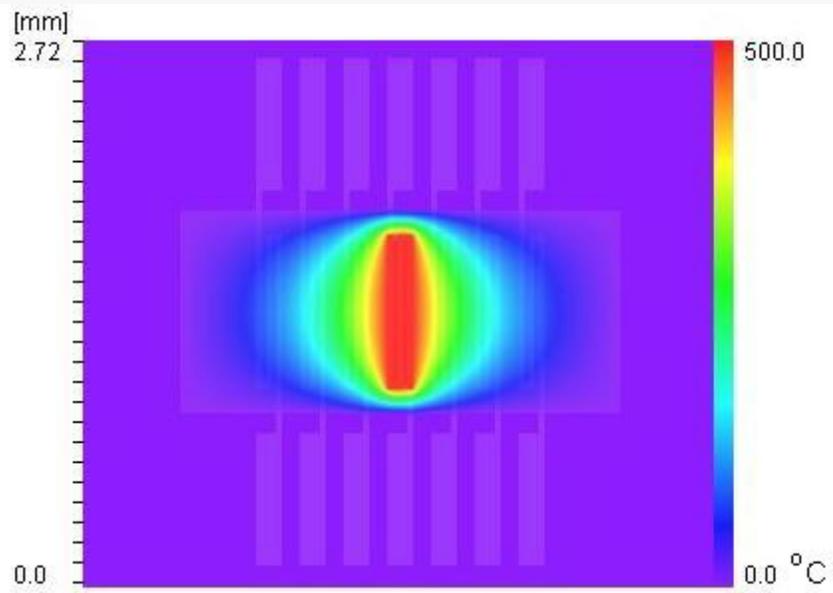
	317 × 273 (uniform grid)
	$\Delta x = \Delta y = \Delta l = 10 \mu m$
B.C.	Dirichlet (Si : 0°C )
	500 °C
	$u, v = 0$

Simulation Conditions

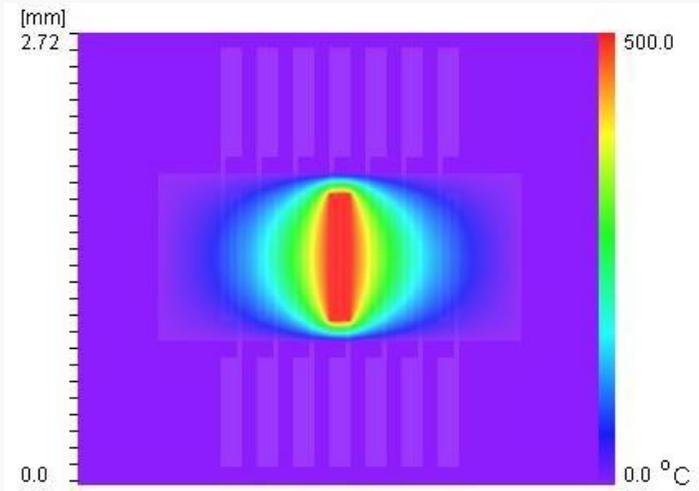
	S <sub>i</sub> (m=0)	S <sub>i</sub> O <sub>2</sub> (m=1)	P <sub>t</sub> (m=2)
k	150	20	71
	2330	2650	21400
c	702.9	753.1	130

Material Constants

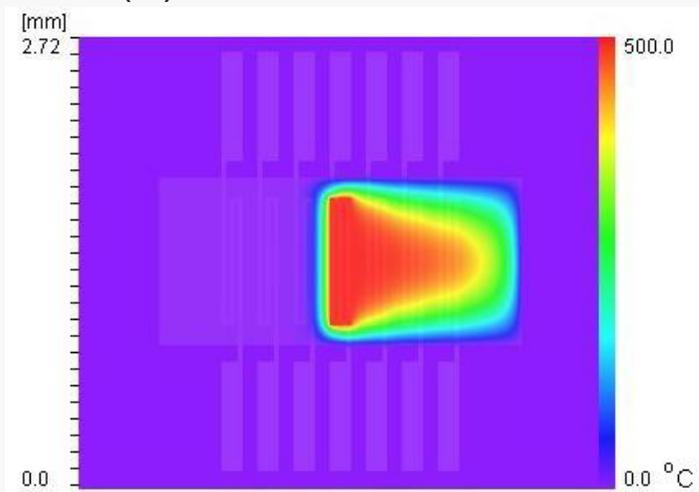
$$\alpha_x = \alpha_y = \alpha_m = \frac{k_m}{\rho_m c_m} \text{ [m}^2\text{/s]}$$



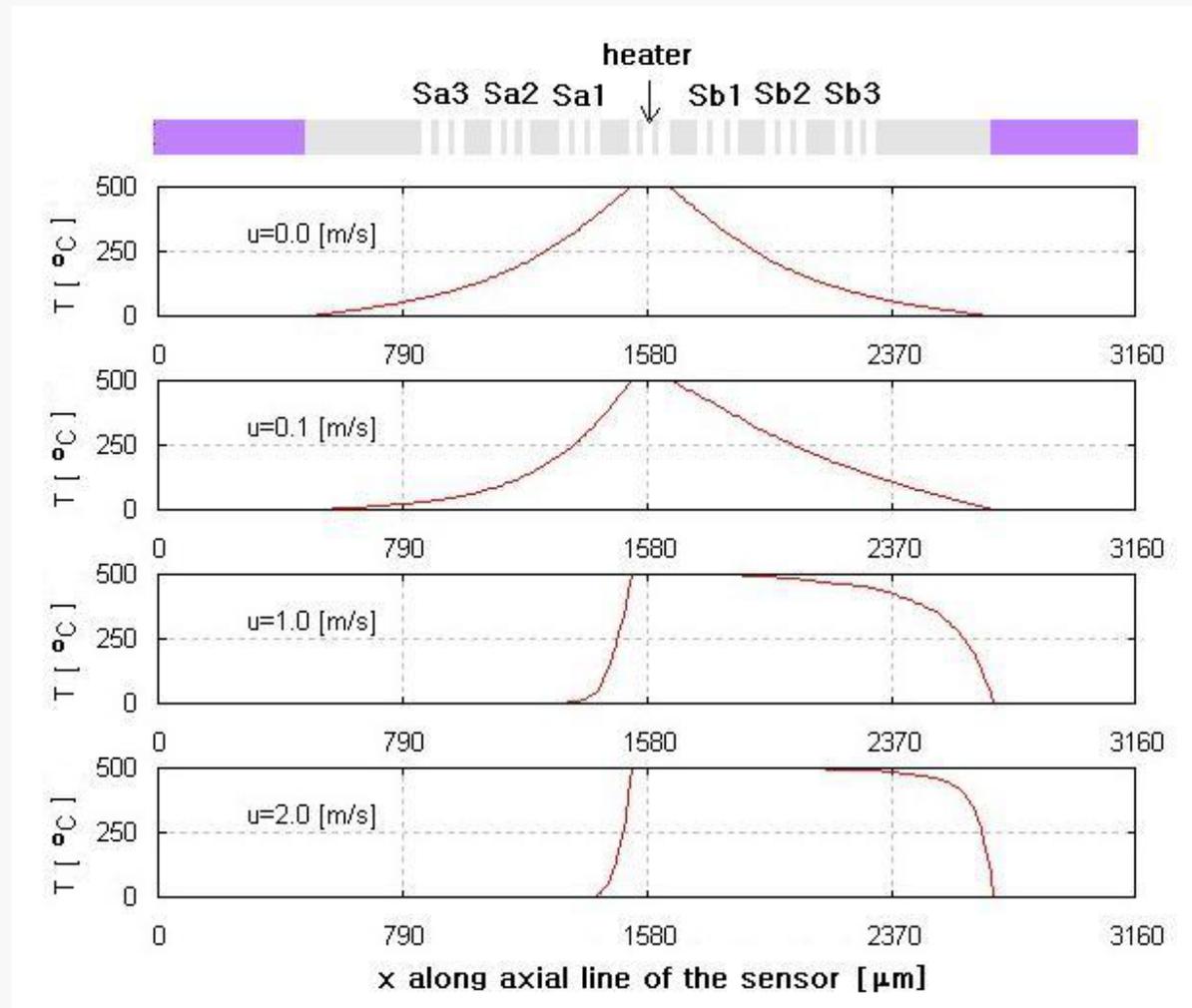
(a) case of  $u=v=0.0$  m/s

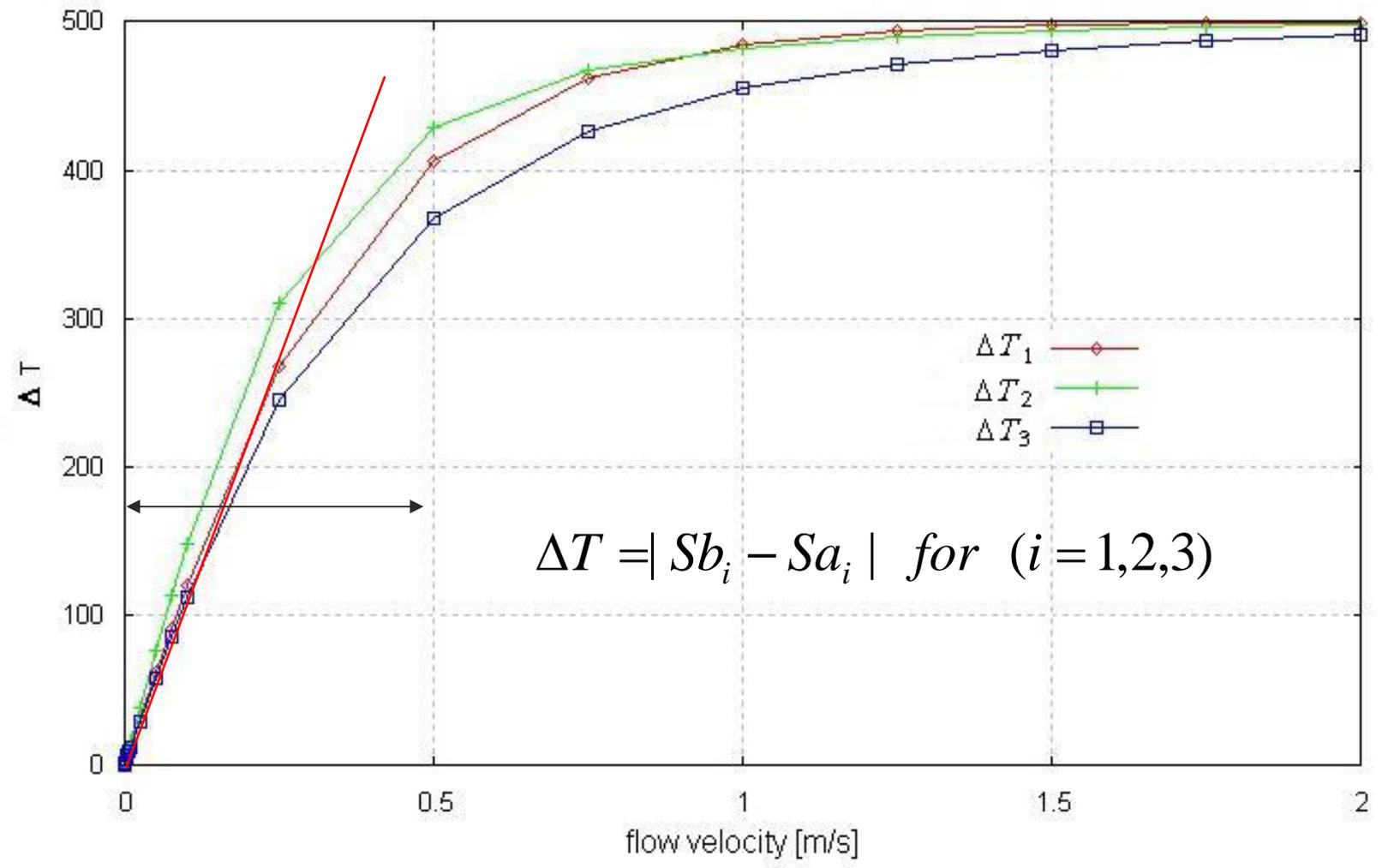


(b)  $u=0.01, v=0.0$  m/s



(c)  $u=1.0, v=0.0$  m/s







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